## **Exclusive and semi-inclusive strangeness and charm production in** *π***N and NN reactions**

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Abstract. Using the Quark-Gluon Strings Model (QGSM) combined with Regge phenomenology we consider the reactions  $\pi^-p \to K^0\Lambda$  and  $\pi^-p \to D^-\Lambda_c^+$  which are dominated by the contributions of the K<sup>\*</sup><br>and  $D^*$  Begge trajectories, respectively. The spin structure of the applitudes is described by introducing and D<sup>∗</sup> Regge trajectories, respectively. The spin structure of the amplitudes is described by introducing Reggeized Born terms. It is found that the existing data for the reaction  $\pi^-p \to K^0\Lambda$  are in reasonable agreement with the model predictions. To describe the absolute values of the cross-sections it is necessary to introduce also suppression factors which can be related to absorption corrections. Furthermore, assuming the  $SU(4)$  symmetry to hold for Regge residues and the universality of absorption corrections we calculate the cross-section of the reaction  $\pi^- p \to D^- \Lambda_c^+$ . Employing the latter results from  $\pi^- p$  reactions<br>we then estimate the contributions of the pion exchange mechanism to the cross-sections of the reactions we then estimate the contributions of the pion exchange mechanism to the cross-sections of the reactions  $NN \to NKA$  and  $NN \to N\bar{D}A_c$  and compare them with the contributions of the K and D exchanges. We find that the  $NN$  reactions are dominated not by pion exchange but by  $K$  and  $D$  exchanges, respectively. Moreover, assuming the  $SU(4)$  symmetry to hold approximately for the coupling constants  $g_{NDA_c} = g_{NKA}$ we analyze also the production of leading  $\Lambda_c$ -hyperons in the reaction  $NN \to \Lambda_c X$ . It is shown that the non-perturbative mechanism should give an essential contribution to the  $\Lambda_c$  yield for  $x \geq 0.5$ .

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Recently it has been argued [1] that the open-charm enhancement observed in nucleus-nucleus collisions [2] at the SPS might be due to secondary reaction mechanisms such as  $\pi N \to \bar{D}A_c$  or  $NN \to N\bar{D}A_c$ . In this work we present estimates of these elementary cross-sections using the anology with strangeness production in  $\pi N$  and NN collisions. We consider also semi-inclusive  $\Lambda$  and  $\Lambda_c$  production in the reactions  $NN \rightarrow NXA$  and  $NN \rightarrow NXA_c$ .

It is well known that the methods of perturbative QCD cannot be applied for a calculation of the cross-sections mentioned above especially at invariant energies closer to threshold. For the analysis of binary reactions we instead use the non-perturbative Quark-Gluon String Model [3] and for reactions with three particles in the final state we employ the meson exchange model taking into account the exchanges of the lowest meson states —pseudoscalar and vector.

The amplitudes for the reactions  $\pi N \rightarrow K\Lambda$  and  $\pi N \to D A_c$  are calculated using the Reggeized–Born-term approach (see, *e.g.*, refs. [4,5]) with contributions of  $K^*$ and  $D^*$  Regge trajectories, respectively. The parameters of the trajectories are taken from ref. [6], whereas for the coupling constants we assume  $SU(4)$  symmetry, as suggested recently by Lin and Ko [7]. With these parameters the energy dependence of the total  $\pi^-p \to K^+ \Lambda$  crosssection (solid line in fig. 1) as well as the  $t$ -dependence of the differential  $\pi^-p \rightarrow K^+ \Lambda$  cross-section are described rather well, except for the region close to threshold where the dominant contribution stems from the well-established s- and p-wave resonances [8]. We note that to obtain the absolute value of the cross-section one has to introduce a suppression factor of  $\sim$  0.4, which can be interpreted as an absorption correction. Assuming its universality we will introduce the same suppression factor for charm production, too. The resulting total cross-section of the reaction  $\pi^- p \to D^- \Lambda_c^+$  is shown by the dashed line in fig. 1.<br>Our next step is to study  $NN$  reactions who

Our next step is to study NN reactions where we first apply our model to strangeness production. Using the method of Yao [9] one can express the  $\pi$  exchange crosssection for the reaction  $pp \to pK^+\Lambda$  in terms of the  $g_{NN\pi}$ 

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**Fig. 1.** Total cross-section for the reaction  $\pi^- p \to K^+ \Lambda$  (solid line) and  $\pi^-p \to D^- \Lambda_c^+$  (dashed line) as a function of the invariant energy above thresholds in comparison to the data invariant energy above thresholds in comparison to the data from ref. [10].

coupling constant and the  $\pi^0 p \to K^+ \Lambda$  cross-section as

$$
\sigma = \frac{g_{NN\pi}^2}{8\pi^2 p_i^2 s} \int_{W_{\text{min}}}^{W_{\text{max}}} k W^2 \sigma(\pi^0 p \to K^+ \Lambda, W) dW
$$
  
 
$$
\times \int_{t_{\text{min}}(W)}^{t^{\text{max}}(W)} F_{\pi}^4(t) \frac{1}{(t - m_{\pi}^2)^2} t dt, \tag{1}
$$

where W is the c.m. energy in the  $K^+A$  subsystem and  $t$  is the 4-momentum transfer squared between the initial and final baryons. The form factor was chosen to be of the standard monopole type:  $F_{\pi}(t) = (A_{\pi}^2 - m_{\pi}^2)/(A_{\pi}^2 - t)$  with  $A = 1.3$  GeV. A similar expression —but with t) with  $\Lambda_{\pi} = 1.3$  GeV. A similar expression —but with  $\sigma(K^+p)$ — can be written for the K exchange. For the  $K^+p$  elastic cross-section employed in this case we use the parametrization of Cugnon *et al.* [11].

The total cross-section of the reaction  $pp \to K^+ \Lambda p$  as a function of the laboratory momentum  $p_{\text{lab}}$  is shown in Fig. 2. The dashed and solid lines describe the  $\pi$ - and  $K$  exchange contributions, respectively, with the cutoff  $\Lambda_K = 1.0$  GeV. An interesting observation is that the pion exchange contribution is substantially smaller than the  ${\cal K}$ exchange and can be neglected especially at higher energies. The reason for that is a difference in the energy dependence of the elementary cross-sections:  $\sigma(\pi^-p \to KA)$ falls off with energy, whereas  $\sigma(K^+p)$  is almost constant since it is dominated by pomeron exchange. Moreover, the  $K$  exchange alone is able to reproduce the experimental data when choosing the cutoff  $\Lambda_K = 1.0 \text{ GeV}.$ 

We see that using the approach of Yao [9] we can express the cross-section for the reaction  $pp \rightarrow K^+pA$ through the coupling constant  $g_{K^+p\Lambda}$  and the elastic  $K^+p$ scattering cross-section  $\sigma_{el}(K^+p)$ . Similarly, the crosssection for the leading- $\Lambda$  production in the reaction  $pp \rightarrow$  $X\Lambda$  can be expressed through the same coupling constant and the total  $K^+p$  scattering cross-section  $\sigma_{\text{tot}}(K^+p)$ .

As follows from fig. 2 the cross-section of the reaction  $pp \rightarrow K^+p\Lambda$  is about 40–50  $\mu$ b for  $p_{\text{lab}} \geq 5$  GeV/c. The



**Fig. 2.** The total cross-section for the reaction  $pp \rightarrow K^+ \Lambda p$  as a function of proton laboratory momentum  $p_{lab}$ . The dashed line denotes the  $\pi$  exchange contribution, while the solid line corresponds to the K exchange with the cutoff  $\Lambda_K = 1.0$  GeV.

ratio of the cross-sections  $\sigma_{tot}(K^+p)/\sigma_{el}(K^+p) \simeq 7-8$ . Thus we expect that the cross-section for semi-inclusive leading-Λ production in the reaction  $pp \rightarrow X\Lambda$  via K exchange should be about  $\sigma_{K-{\rm exch}}(pp \rightarrow X\Lambda) \simeq 300-$ 400  $\mu$ b. Furthermore, the ratio of the coupling constants  $g_{K^*+p\Lambda}/g_{K^+p\Lambda} \simeq 2$  [5], which implies that the contribution of the  $K^*$  exchange to the cross-section of the leading-Λ production might be <sup>∼</sup> 4 times larger. Thus, we expect the cross-section for the semi-inclusive leading-Λ production to be about

$$
\sigma_{K\text{-exch}}(pp \to X\Lambda) + \sigma_{K\text{*-exch}}(pp \to X\Lambda) \simeq 1.5\text{-}2\,\text{mb}.
$$

We note that Erhan *et al.* [12] quote total cross-sections  $\sqrt{s}$  = 53 and 62 GeV, respectively. This comparison shows<br>that the mechanism considered above gives a dominant for the reaction  $pp \rightarrow A + X$  of  $4.\overline{4} \pm 0.2$  and  $4.7 \pm 0.2$  mb at that the mechanism considered above gives a dominant contribution to the semi-inclusive leading-Λ production in the reaction  $pp \to X\Lambda$ .

Using the analogy of strangeness and charm production we can expect that the main contributions to the cross-sections of the reactions  $NN \to \bar{D}_c (\bar{D}_c^*) A_c N$  come from the  $D_c$  and  $D^*$  exchanges respectively. The coufrom the  $D_c$  and  $D_c^*$  exchanges, respectively. The cou-<br>pling constants —involving a charm quark— can be repling constants —involving a charm quark— can be related to the strange ones using SU(4) symmetry, *i.e.*  $g_{KNA} = g_{D_cNA_c}$  and  $g_{K^*+NA} = g_{D_c^*NA_c}$ . Within the approach of Yao [9] we then can express the cross-section proach of Yao [9] we then can express the cross-section of the reaction  $p p \to \bar{D}_c^0 p A_c^+$  through the coupling con-<br>stant  $g_{\pm 0} \to$  and the elastic  $\bar{D}_c^0 p$  scattering cross-section stant  $g_{\bar{D}_c^0 p A_c^+}$  and the elastic  $\bar{D}_c^0 p$  scattering cross-section  $\sigma_{el}(\bar{D}_e^0 p)$ . Similarly, the cross-section for the leading- $A_c$ <br>production in the reaction  $p p \to X A_c$  can be expressed production in the reaction  $pp \rightarrow X A_c$  can be expressed through the same coupling constant and the total  $\bar{D}_c^0 p$ <br>scattering cross-section  $\sigma_{\rm tot}(\bar{D}_c^0 p)$ scattering cross-section  $\sigma_{\text{tot}}(\bar{D}_c^0 p)$ .<br>In our calculations we assume

In our calculations we assume  $\sigma_{el}(\bar{D}_c^0 p) = \sigma_{el}(K^+p)$ <br> $\sigma_{el}(\bar{D}_c^0 p) = \sigma_{el}(K^+p)$  while the form factor is taken and  $\sigma_{\rm tot}(\bar{D}_c^0 p) = \sigma_{\rm tot}(K^+p)$ , while the form factor is taken as

$$
F_D(t) = \Lambda_D^2 / (\Lambda_D^2 - t). \tag{2}
$$

 $F_D(t) = A_D^2/(A_D^2 - t).$ <br>In fig. 3 we present the total cross-section for the reaction  $pp \rightarrow \overrightarrow{D}_c^0 \Lambda_c^+ p$  as a function of the invariant energy



**Fig. 3.** The predicted total cross-section for the reaction  $pp \rightarrow \bar{D}^0 \Lambda_c^+ p$  as a function of the invariant energy above<br>threshold. The dash-dotted line denotes the contribution from threshold. The dash-dotted line denotes the contribution from the  $\pi$  exchange, while the solid line and the dashed line correspond to the  $D_c$  exchange with the cutoff  $\Lambda_D = 1.0$  GeV and <sup>1</sup>.5 GeV, respectively.

above threshold for  $\Lambda_{D_0} = 1.5$  GeV (dashed line) and  $\Lambda_{D_c} = 1.0$  GeV (solid line). The dash-dotted line denotes the contribution from the  $\pi$  exchange alone. Note that for the elementary reaction  $\pi^0 p \to \bar{D}^0 \Lambda_c^+$  we use the am-<br>plitude calculated in the approach discussed above while plitude calculated in the approach discussed above, while for the  $\bar{D}^0 p$  cross-section we adopt a value corresponding to the asymptotic  $K^+p$  cross-section, *i.e.*  $\sim$  3 mb, which is consistent with the values used in the literature (see, *e.g.*, [13]).

We find that the main contribution to the cross-section for the reaction  $NN \to \bar{D}A_cN$  (a few GeV above threshold) comes from the  $D_c$  exchange which is much larger than the pion exchange for cutoff parameters  $\Lambda_D \geq 1$  GeV.

To find restrictions on the cutoff parameter  $\Lambda_D$  in (2) we use the data from ref. [14] on semi-inclusive  $\Lambda_c$  production in the reaction  $pp \to X A_c$ . We assume now that the same D exchange mechanism also gives a large contribution to the semi-inclusive  $\Lambda_c$  production at x close to 1. (In fact, in our calculation the cross-section is peaked at  $x \sim 0.9$ .) Of course, in this case one has to insert the total  $\bar{D}^0p$  cross-section in the corresponding analog of eq. (1). As shown in fig. 4 the  $p_t$  dependence of the differential cross-section constrains  $\Lambda_D$  to 1–1.5 GeV.

To make a rough estimate of the absolute value of the D exchange contribution to the leading- $A_c$  production in the reaction  $pp \rightarrow X\Lambda_c$  we assume that the total  $\bar{D}^0p$ cross-section is the same as in case of  $K^+p$  scattering, *i.e.*  $\sim$  20 mb. Then at c.m. energies larger than 10 GeV we obtain a cross-section of  $\sim$  10–40  $\mu$ b depending on the choice of the cutoff. As in the case of strangeness production the contribution from  $D^*$  exchange might be approximately 4 times larger. Therefore, according to our estimates the cross-section of the semi-inclusive leading- $A_c$  production at high energy should be as large as  $\sim$  50–200 µb. This estimate agrees with the experimental value of  $40-200 \mu b$ 



**Fig. 4.** The  $p_t$  dependence of the differential cross-section for the reaction  $pp \rightarrow X A_c$  at  $\sqrt{s} = 62$  GeV. The theoretical curves correspond to the differential cross-section  $d^2\sigma/dp_t^2 dx$ <br>calculated at  $x = 0.9$  (where it peaks) for the cutoffs  $A_D =$ calculated at  $x = 0.9$  (where it peaks) for the cutoffs  $\Lambda_D =$ 1.0 GeV (solid line),  $A_D = 1.3$  GeV (dashed line),  $A_D =$ <sup>1</sup>.5 GeV (dash-dotted line). The results are normalized to the data from [14] at small transverse momentum  $p_t$ .

at  $\sqrt{s}$  = 62 GeV quoted in ref. [14] which implies that the non-perturbative mechanism considered here gives an essential contribution to the leading- $A_c$  production.

We finally note, that the same mechanism with  $D$  and  $D^*$  exchanges should provide a similar contribution to the open-charm production in  $p\bar{p}$  collisions.

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